New examples on Lavrentiev gap using fractals

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We construct new examples on Lavrentiev phenomenon using fractal contact sets. Comparing to the well-known examples of Zhikov it is not important that at the saddle point the variable exponent crosses the threshold dimension. As a consequence we give the negative answer to the well-known conjecture that the dimension plays a critical role for the Lavrentiev gap to appear. We apply our method to the setting of variable exponents, the double phase potential and weighted *p*-energy.

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