

Grid creation and visualization

This notebook shows how to perform grid creation and visualization with the assistance of the packages `ExtendableGrids.jl` and `SimplexGridFactory.jl`. Visualization in this notebook is done using the `GridVisualize.jl` package.

```

begin
using SimplexGridFactory
using ExtendableGrids
using Triangulate
using TetGen
using GridVisualize
using PlutoVista
using PlutoUI
default_plotter!(PlutoVista)
using PyPlot
end

```

1D grids

1D grids are created just from arrays of monotonically increasing coordinates using the `simplexgrid` method.

```

X1 = 0.0:0.1:1.0
X1=range(0,1,length=11)

```

```

g1 = ExtendableGrids.ExtendableGrid{Float64, Int32};
dim: 1 nodes: 11 cells: 10 bfaces: 2

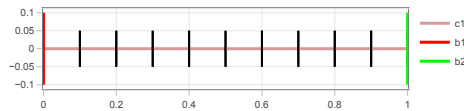
```

```

g1=simplexgrid(X1)

```

We can plot a grid with a method from `GridVisualize.jl`



```

gridplot(g1; resolution=(500,150),legend=:rt)

```

We see some additional information:

- `cellregion`: each grid cell (interval, triangle, tetrahedron) as an integer region marker attached
- `bfaceregion`: boundary faces (points, lines, triangles) have an integer boundary region marker attached

We can also have a look into the grid structure:

```

Dict{CellRegions => [1, 1, 1, 1, 1, 1, 1, 1, 1, 1], NumBFaceRegions => 2, CellNodes => 2x1f
1
2

```

```

g1.components

```

Components can be accessed via `[]`. In fact the keys in the dictionary of components are `types`.

```

1x11 Matrix{Float64}:
0.0 0.1 0.2 0.3 0.4 0.5 0.6 0.7 0.8 0.9 1.0

```

```

g1[Coordinates]

```

```

2x10 Matrix{Int32}:
1 2 3 4 5 6 7 8 9 10
2 3 4 5 6 7 8 9 10 11

```

```

g1[CellNodes]

```

Modifying region markers

The `simplexgrid` method provides a default distribution of markers, but we would like to be able to change them. This can be done by putting masks on cells or faces (points in 1D):

```

g2 = ExtendableGrids.ExtendableGrid{Float64, Int32};
dim: 1 nodes: 11 cells: 10 bfaces: 2

```

```

g2=deepcopy(g1)

```

```

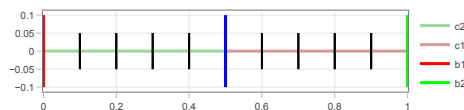
cellmask!(g2, [0.0], [0.5], 2);

```

```

bfacemask!(g2, [0.5],[0.5], 3);

```



```

gridplot(g2; resolution=(500, 150),legend=:rt)

```

Creating locally refined grids

For this purpose, we just need to create arrays with the corresponding coordinate values. This can be done programmatically.

Two support methods are provided for this purpose.

0.1

```
· hmin=0.01 ; hmax=0.1
```

The `geospace` method creates an array such that the smallest interval size is `hmin` and the largest interval size is not larger but close to `hmax`, and the interval sizes constitute a geometric sequence.

`X2L =`

```
[0.0, 0.0931551, 0.170501, 0.234722, 0.288044, 0.332316, 0.369076, 0.399597, 0.424939, 0.4
```

```
· X2L=geospace(0,0.5,hmax,hmin)
```

`DX2 =`

```
[0.0931551, 0.0773463, 0.0642203, 0.0533218, 0.0442729, 0.0367596, 0.0305213, 0.0253417, 0
```

```
· DX2=X2L[2:end]-X2L[1:end-1]
```

```
[1.20439, 1.20439, 1.20439, 1.20439, 1.20439, 1.20439, 1.20439, 1.20439, 1.20439, 1.20439,
```

```
· DX2[1:end-1]./DX2[2:end]
```

`X2R =`

```
[0.5, 0.51, 0.522044, 0.536549, 0.55402, 0.575061, 0.600403, 0.630924, 0.667684, 0.711956,
```

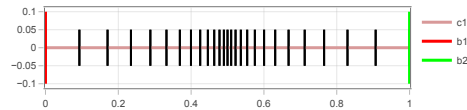
```
· X2R=geospace(0.5,1,hmin,hmax)
```

We can glue these arrays together and create a grid from them:

`X2 =`

```
[0.0, 0.0931551, 0.170501, 0.234722, 0.288044, 0.332316, 0.369076, 0.399597, 0.424939, 0.4
```

```
· X2=glue(X2L,X2R)
```



```
· gridplot(simplexgrid(X2); resolution=(500,150),legend=:rt)
```

Plotting functions

We assume that functions can be represented by their node values and plotted via their piecewise linear interpolants. E.g. they could come from some simulation.

```
g1d2 = ExtendableGrids.ExtendableGrid{Float64, Int32};  
dim: 1 nodes: 201 cells: 200 bfaces: 2
```

```
· g1d2=simplexgrid(range(-10,10,length=201))
```

`fsin =`

```
[0.544021, 0.457536, 0.366479, 0.271761, 0.174327, 0.0751511, -0.0247754, -0.124454, -0.22
```

```
· fsin=map(sin,g1d2)
```

`fcos =`

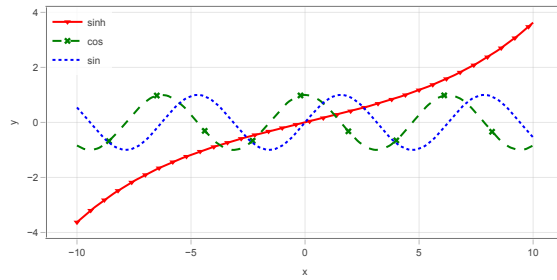
```
[-0.839072, -0.889191, -0.930426, -0.962365, -0.984688, -0.997172, -0.999693, -0.992225, -
```

```
· fcos=map(cos,g1d2)
```

`fsinh =`

```
[-3.62686, -3.55234, -3.47923, -3.40752, -3.33718, -3.26816, -3.20046, -3.13403, -3.06886,
```

```
· fsinh=map(x->sinh(0.2*x), g1d2)
```



```

    . let
      vis=GridVisualizer(;resolution=(600,300),legend=:lt)
      .
      .
      scalarplot!(vis, gid2, fsinh, label="sinh", markershape=:dtriangle,
        color=:red,markevery=5,clear=false)
      .
      scalarplot!(vis, gid2, fcos, label="cos", markershape=:xcross, color=:green,
        linestyle=:dash, clear=false,markevery=20)
      .
      scalarplot!(vis, gid2, fsin, label="sin", markershape=:none, color=:blue,
        linestyle=:dot, clear=false, markevery=20)
      .
      reveal(vis)
    . end

```

2D grids

Tensor product grids

For 2D tensor product grids, we can again use the `simplexgrid` method and apply the mask methods for modifying cell and boundary region markers.

```

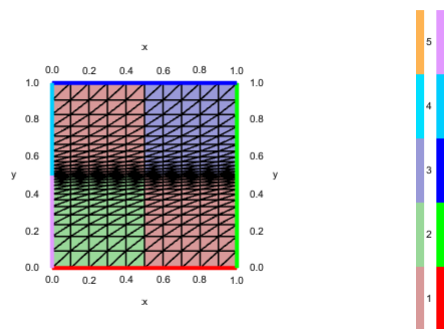
ExtendableGrids.ExtendableGrid{Float64, Int32};
dim: 2 nodes: 297 cells: 520 bfaces: 72

```

```

    . begin
      g2d1=simplexgrid(X1,X2)
      cellmask!(g2d1, [0.0,0.0], [0.5, 0.5], 2)
      cellmask!(g2d1, [0.5,0.5], [1.0, 1.0], 3)
      bfacemask!(g2d1, [0.0, 0.0], [0.0, 0.5],5)
    . end

```



```

    . gridplot(g2d1,resolution=(600,400),linewidth=0.5,legend=:lt)

```

To interact with the plot, you can use the mouse wheel or double touch to zoom, "shift-mouse-left" to pan, and "alt-mouse-left" or "ctrl-mouse-left" to reset.

We can also have a look into the components of a 2D grid:

```

Dict{CellRegions} => [2, 2, 2, 2, 2, 2, 2, 2, 2, more ], NumBFaceRegions => 5, CellNode

```

```

    . g2d1.components

```

Unstructured grids

For the triangulation of unstructured grids, we use the mesh generator `Triangle` via the `Triangulate.jl` and `SimplexGridFactory.jl` packages.

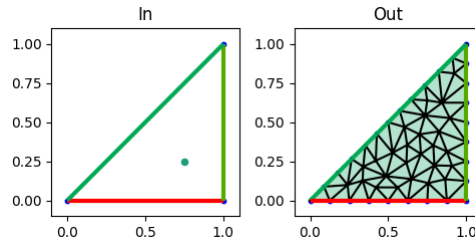
The later package exports the `SimplexGridBuilder` which shall help to simplify the creation of the input for `Triangulate`.

```
builder2 =
  SimplexGridBuilder(Triangulate, 3, 1, 1.0, 1.0e-12, [1, 2, 3], [[1, 2], [2, 3], [3, 1]], Bi
```

```

- builder2=let
-   b=SimplexGridBuilder(Generator=Triangulate)
-   p1=point!(b,0,0)
-   p2=point!(b,1,0)
-   p3=point!(b,1,1)
-
-   # Specify outer boundary
-   facetregion!(b,1)
-   facet!(b,p1,p2)
-   facetregion!(b,2)
-   facet!(b,p2,p3)
-   facetregion!(b,3)
-   facet!(b,p3,p1)
-
-   cellregion!(b,1)
-   regionpoint!(b,0.75,0.25)
-
-   options!(b,maxvolume=0.01)
-   b
- end
```

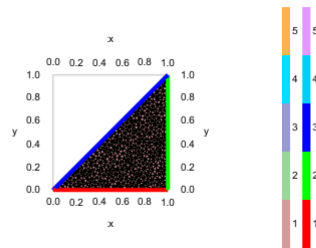
We can plot the current state of the builder (in the moment this works only with PyPlot):



```
- builderplot(builder2,Plotter=PyPlot)
```

```
grid2d2 = ExtendableGrids.ExtendableGrid{Float64, Int32};
dim: 2 nodes: 449 cells: 793 bfaces: 103
```

```
- grid2d2=simplexgrid(builder2;maxvolume=0.001)
```



```
- gridplot(grid2d2, resolution=(400,300), linewidth=0.5)
```

More complicated grids

More complicated grids include:

- local refinement
- interior boundaries
- different region markers
- holes

The particular way to describe these things is due to Jonathan Shewchuk and his mesh generator [Triangle](#) via its Julia wrapper package [Triangulate.jl](#).

Local refinement

```
refinement_center = [0.8, 0.2]
- refinement_center=[0.8,0.2]
```

For local refinement, we define a function, which is able to tell if a triangle is to be refined ("unsuitable") or can be kept as it is.

The function measures the distance between the refinement center and the triangle barycenter. We require that the area increases with the distance from the refinement center.

```

- function unsuitable(x1,y1,x2,y2,x3,y3,area)
-   bary_x=(x1+x2+x3)/3.0
-   bary_y=(y1+y2+y3)/3.0
-   dx=bary_x-refinement_center[1]
-   dy=bary_y-refinement_center[2]
-   qdist=dx^2+dy^2
-   area>0.1*max(1.0e-2,qdist)
- end;
```

Interior boundaries

Interior boundaries are described in a similar as exterior ones - just by facets connecting points.

Subregions

Subregions are defined as regions surrounded by interior boundaries. By placing a "region point" into such a region and specifying a "region number", we can set the cell region marker for all triangles created in the subregion.

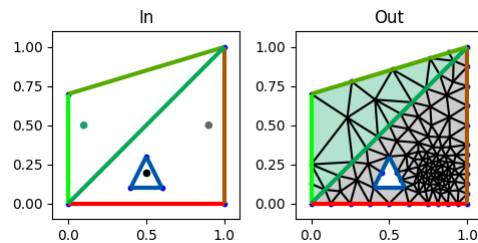
Holes

Holes are defined in a similar way as subregions, but a "hole point" is placed into the place which shall become the hole.

```

- builder3=let
-   b=SimplexGridBuilder(Generator=Triangulate;tol=1.0e-10)
-
-   # Specify points
-   p1=point!(b,0,0)
-   p2=point!(b,1,0)
-   p3=point!(b,1,1)
-   p4=point!(b,0,0.7)
-
-   # Specify outer boundary
-   facetregion!(b,1)
-   facet!(b,p1,p2)
-   facetregion!(b,2)
-   facet!(b,p2,p3)
-   facetregion!(b,3)
-   facet!(b,p3,p4)
-   facetregion!(b,4)
-   facet!(b,p1,p4)
-
-   # Activate unsuitable callback
-   options!(b,unsuitable=unsuitable)
-
-   # Specify interior boundary
-   facetregion!(b,5)
-   facet!(b,p1,p3)
-
-   # Coarse elements in upper left region #1
-   cellregion!(b,1)
-   maxvolume!(b,0.1)
-   regionpoint!(b,0.1,0.5)
-
-   # Fine elements in lower right region #2
-   cellregion!(b,2)
-   maxvolume!(b,0.01)
-   regionpoint!(b,0.9,0.5)
-
-   # Hole
-   hp1=point!(b,0.4,0.1)
-   hp2=point!(b,0.6,0.1)
-   hp3=point!(b,0.5,0.3)
-   holepoint!(b,0.5,0.2)
-   facetregion!(b,6)
-   facet!(b,hp1,hp2)
-   facet!(b,hp2,hp3)
-   facet!(b,hp3,hp1)
-
-   b
- end;

```

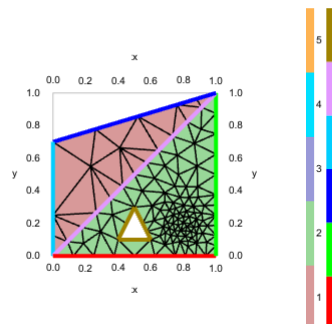


```
- builderplot(builder3,Plotter=PyPlot)
```

Create a simplex grid from the builder

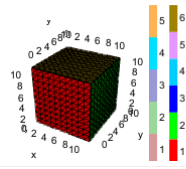
```
grid2d3 = ExtendableGrids.ExtendableGrid{Float64, Int32};
dim: 2 nodes: 117 cells: 199 bfaces: 47
```

```
- grid2d3=simplexgrid(builder3)
```



```
- gridplot(grid2d3,legend=:lt, resolution=(400,400))
```

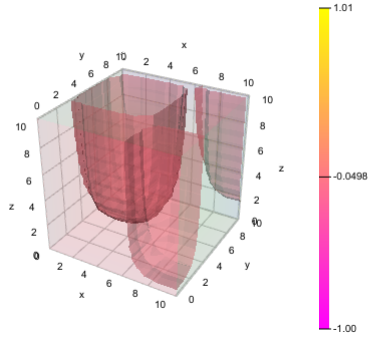

p3dg =



```
p3dg=GridVisualizer(dim=3,resolution=(200,200))
```

```
gridplot!(p3dg,grid3d1,zplanes=[zplane],yplanes=[yplane], xplanes=[xplane],
resolution=(200,200),show=true)
```

p3ds =



```
p3ds=GridVisualizer(dim=3,resolution=(400,400))
```

```
scalarplot!(p3ds,grid3d1, func3, zplanes=[zplane], yplanes=[yplane],xplanes=[xplane],
levels=[flevel],colormap=:spring,resolution=(200,200),show=true,levelalpha=0.5,outlinealpha=0.1)
```

f= -0.049773893527225145

x= 10.1

y= 10.1

z= 10.1

```
md"""
f=@bind flevel
Slider(range(extrema(func3)...,length=20),default=mean(func3),show_value=true)
x=@bind xplane Slider(X3[1]:0.1:X3[end],default=X3[end],show_value=true)
y=@bind yplane Slider(X3[1]:0.1:X3[end],default=X3[end],show_value=true)
z=@bind zplane Slider(X3[1]:0.1:X3[end],default=X3[end],show_value=true)
"""
```

mean (generic function with 1 method)

```
mean(x)=sum(x)/length(x)
```

Unstructured grids

The SimplexGridBuilder API supports creation of three-dimensional grids in way very similar to the 2D case. Just define points with three coordinates and planar (!) facets with at least three points to describe the geometry.

The backend for mesh generation in this case is the [TetGen](#) mesh generator by Hang Si from WIAS Berlin and its Julia wrapper [TetGen.jl](#).

```

- builder3d=let
-
-   b=SimplexGridBuilder(Generator=TetGen)
-
-   p1=point!(b,0,0,0)
-   p2=point!(b,1,0,0)
-   p3=point!(b,1,1,0)
-   p4=point!(b,0,1,0)
-   p5=point!(b,0,0,1)
-   p6=point!(b,1,0,1)
-   p7=point!(b,1,1,1)
-   p8=point!(b,0,1,1)
-
-   facetregion!(b,1)
-   facet!(b,p1 ,p2 ,p3 ,p4)
-   facetregion!(b,2)
-   facet!(b,p5 ,p6 ,p7 ,p8)
-   facetregion!(b,3)
-   facet!(b,p1 ,p2 ,p6 ,p5)
-   facetregion!(b,4)
-   facet!(b,p2 ,p3 ,p7 ,p6)
-   facetregion!(b,5)
-   facet!(b,p3 ,p4 ,p8 ,p7)
-   facetregion!(b,6)
-   facet!(b,p4 ,p1 ,p5 ,p8)
-
-
-   hp1=point!(b,0.4,0.4,0.4)
-   hp2=point!(b,0.6,0.4,0.4)
-   hp3=point!(b,0.6,0.6,0.4)
-   hp4=point!(b,0.4,0.6,0.4)
-   hp5=point!(b,0.4,0.4,0.6)
-   hp6=point!(b,0.6,0.4,0.6)
-   hp7=point!(b,0.6,0.6,0.6)
-   hp8=point!(b,0.4,0.6,0.6)
-
-   facetregion!(b,7)
-   facet!(b,hp1 ,hp2 ,hp3 ,hp4)
-   facet!(b,hp5 ,hp6 ,hp7 ,hp8)
-   facet!(b,hp1 ,hp2 ,hp6 ,hp5)
-   facet!(b,hp2 ,hp3 ,hp7 ,hp6)
-   facet!(b,hp3 ,hp4 ,hp8 ,hp7)
-   facet!(b,hp4 ,hp1 ,hp5 ,hp8)
-   holepoint!(b ,0.5,0.5,0.5)
-
-
-   b
-
- end;

```

```

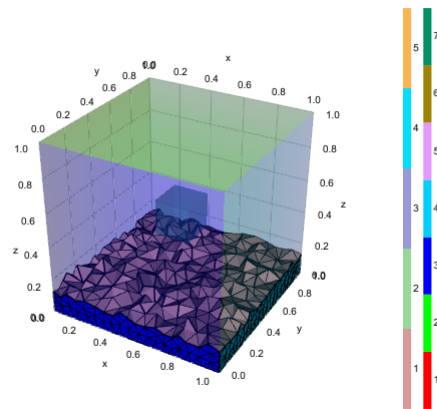
grid3d2 = ExtendableGrids.ExtendableGrid{Float64, Int32};
dim: 3 nodes: 4650 cells: 21311 bfaces: 4890

```

```

- grid3d2=simplexgrid(builder3d,maxvolume=0.0001)

```



```

- gridplot(grid3d2,zplane=0.1,azim=20,elev=20,linewidth=0.5,outlinealpha=0.3)

```

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